

MATH 119 PRACTICE SECOND MIDTERM

The actual midterm will of course be shorter than this. It will contain at least one question taken directly off your homework. You may use a calculator, but **not any of its calculus functions**.

- Section 8.8 (p. 426): #5. Chapter 8 Review (p. 428): #17, 21, 37, 55.
- Sarah Series would like to set up a scholarship for Math 119 students, to be awarded each year, starting in one year (sorry). How much money would she have to deposit in an account which earns 7% interest a year (compounded continuously; that is, if she deposits $\$D$, then after t years she'll have $\$De^{0.07t}$) in order to award a $\$1,000$ scholarship each year? (HINT: As is usually the case with word problems, it helps to break the problem into small pieces. First compute how much Sarah would need to deposit now in order to award a $\$1,000$ scholarship next year. Then add in the amount that Sarah would need to deposit in order to award a $\$1,000$ scholarship in two years. And so on. . .)

- Determine if the following series converge or diverge. Be sure to give reasons!

(a)
$$\sum_{n=1}^{\infty} \frac{2n^4 - 6n^3 + 13n}{n^5 + n^2 + 4}$$

(b)
$$\sum_{n=1}^{\infty} \frac{1}{3^{n-1} + 1}$$

(c)
$$\sum_{n=2}^{\infty} \frac{(n!)(n!)}{(2n)!}$$

(d)
$$\sum_{n=1}^{\infty} \left(1 + \frac{2}{n}\right)^n$$

(e)
$$\sum_{n=1}^{\infty} \frac{(-1)^n n^2}{2^n}$$

(f)
$$\sum_{n=1}^{\infty} a_n$$
, if the n th partial sum of this series is given by $s_n = \frac{n-1}{2n+1}$.

(g)
$$\sum_{n=1}^{\infty} \frac{n+1}{n} a_n$$
, if you know that $\sum_{n=1}^{\infty} a_n$ is a positive series that converges.

- Find positive numbers A and B such that $0 < A \leq \sum_{n=0}^{\infty} \frac{1}{5^n + n^3} \leq B$.

- Use a third-degree Taylor polynomial to estimate $\sqrt{1.1}$.

- Compute $1/e$ to within $1/10$ of its actual value. Be sure to explain how you can be sure of the accuracy of your estimate. (HINT: $1/e = e^{-1}$, and $e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$)

- Find the radius of convergence of the power series $\sum_{n=0}^{\infty} \frac{x^{2n}}{4^n}$.

- A rod of length 3 meters and density $\delta(x) = 2 + \cos x$ grams/meter is positioned along the x -axis with its left end at the origin.

- Where is the rod most dense?
- Where is the rod least dense?
- Is the center of mass of this rod closer to the origin, or closer to $x = 3$?
- What is the total mass of the rod?
- Where is the center of mass of the rod?